# LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600034 

B.Sc. \& B.Com. DEGREE EXAMINATION - MATHS, PHYSICS \& COMMERCE

THIRD SEMESTER - NOVEMBER 2015

## ST 3205-ADVANCED STATISTICAL METHODS

Max. : 100 Marks

## PART A

## Answer ALL the questions:

( $10 \times 2=20$ )

1) Write down the formula for Yule's coefficient of association.
2) Check the consistency of the data, $N=80,(A)=40,(B)=50,(A B)=45$.
3) Define probability mass function.
4) Define mutually exclusive events.
5) Define level of significance.
6) Write the test statistic of test for specified proportion.
7) Fill in the blanks:

| Source | d.f | S.S | M.S.S | F-ratio |
| :---: | :---: | :---: | :---: | :---: |
| Treatment | 2 | 168.5 | - | - |
| Error | - | - | 22.83 |  |
| Total | 11 | 374 |  |  |

8) State any two situations where Poisson law can be applied.
9) Write any two uses of control chart.
10) Write down the control limits of R-chart.

## PART B

Answer any FIVE of the following:
( $5 \times 8=40$ )
11) Out of 900 persons, 300 were literate and 400 had travelled beyond the limits of their district. 100 of the literates were among those who had not travelled. Is there any relation between literacy and travelling?
12) A random variable $X$ has the following probability function.

| X | 0 | 1 | 2 | 3 | 4 | 5 |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{P}(\mathrm{x})$ | 0 | k | k | 2 k | $3 \mathrm{k}^{2}$ | $3 \mathrm{k}^{2}+\mathrm{k}$ |

Find (i) $k$, (ii) $\mathrm{P}(\mathrm{X}<4)$, (iii) $\mathrm{P}(\mathrm{X} \geq 2)$, (iv) $\mathrm{P}(1 \leq \mathrm{X} \leq 4)$.
13) State any five properties of normal distribution.
14) Number of road accidents during a month follows Poisson distribution with mean 6 . Find the probability that in a certain month number of accidents will be (i) not more than 3 and (ii) between 2 and 5 and (iii) atleast 2?
15) A person buys 100 electric tubes from two well known makes taken at random from stocks for testing purpose. He finds that make A has a mean life of 1300 hours with a S.D of 82 hours and make B has mean life of 1248 hours with a S.D of 93 hours. Discuss the significance of these results to test which make of electric tubes should the person buy.
16) A random sample of 10 boys has the following I.Qs : 70, 120, 110, 101, 88, 83, 95, 98, 107, 100. Do these data support the assumption of a population mean IQ of 100 ?
17) The following table gives the yields of 15 samples of plot under three varieties of seed.

| A | B | C |
| :---: | :---: | :---: |
| 20 | 18 | 25 |
| 21 | 20 | 28 |
| 23 | 17 | 22 |
| 16 | 15 | 28 |
| 20 | 25 | 32 |

Test using analysis of variance whether there is a significant difference in the average yield of seeds.
18) The following table gives the number of defects in ten woolen carpets manufactured.

| S.no. | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of defects | 3 | 4 | 5 | 6 | 3 | 3 | 5 | 3 | 6 | 2 |

Draw a c-chart and comment on it.

## PART C

## Answer any TWO of the following:

19) (a) From the data given below, calculate the coefficient of contingency between the Heights of husbands and wives.

| Husband | Wives |  |  |
| :---: | :---: | :---: | :---: |
|  | Tall | Medium | Short |
| Tall | 30 | 50 | 20 |
| Medium | 20 | 30 | 10 |
| Short | 10 | 20 | 10 |

(b) Let $\mathrm{U}_{1}, \mathrm{U}_{2}, \mathrm{U}_{3}$ be 3 urns with two red and one black, three red and two black and one red and one black ball respectively. One of the urns is chosen at random and a ball is drawn from it. The color of the ball is found to be black. What is the probability that it has been chosen from $\mathrm{U}_{2}$ ?
20) (a) The incidence of occupational disease in an industry is such that the workmen have a $20 \%$ chance of suffering from it. What is the probability that out of six workmen,
(i) 4 or more will contract the disease and (ii) not more than 1 will contract the disease?
(b) The life of a certain kind of electronic device has a mean of 300 hours and a standard deviation of 25 hours. Assuming that the distribution of life times which are measured to the nearest hour can be approximated closely with a normal curve, (i) find the probability that any one of these device will have a lifetime of more than 350 hours, (ii) what percentage will have life time from 220 and 260 hours? And (iii) find the probability that the devices will have lifetime between 260 and 350 ?
21) (a) A sample of 600 parts manufactured by a factory, the number of defective parts was found to be 45. The company however claimed that only $5 \%$ of their product is defective. Is the claim tenable?
(b) Construct a $\bar{X}$ and R chart for the following data:

| $\mathrm{X}_{1}$ | 22 | 24 | 24 | 25 | 21 | 20 | 25 | 26 | 27 | 21 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{X}_{2}$ | 33 | 31 | 28 | 29 | 28 | 30 | 31 | 32 | 33 | 31 |
| $\mathrm{X}_{3}$ | 33 | 27 | 26 | 25 | 32 | 20 | 27 | 28 | 29 | 20 |

Comment on it.
22) Five types of fertilizers are applied to four varieties of potatoes, each planted on five plots of land of the same size and fertility. The yield are shown in the following table:

| Potatoes | Fertilizer |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D | E |
| I | 34 | 38 | 44 | 40 | 42 |
| II | 50 | 38 | 46 | 52 | 44 |
| III | 42 | 36 | 50 | 46 | 48 |
| IV | 38 | 44 | 52 | 36 | 42 |

Test whether (i) the effect of fertilizers and (ii) the effect of potato varieties are significant on the yield of potatoes?

